

Compound Interest

$$P_n = P_0(1 + r/k)^{Nk}$$

P_n is the _____.

P_0 is the starting balance of the account (also called initial deposit, or _____)

r is the _____ in decimal form

k is the _____ in one year

If the compounding is done annually (once a year), $k = 1$.

If the compounding is done quarterly, $k = 4$.

If the compounding is done monthly, $k = 12$.

If the compounding is done daily, $k = 365$.

Question

An investment account offers an annual interest rate of 5%, compounded semiannually, to encourage long-term savings. Suppose you deposit \$7,500 into the account. How much will the account balance be after 10 years?

Example

A new savings bond offers a fixed interest rate and compounds quarterly, providing an attractive option for long-term investments. Suppose you invest \$5,000 in a savings bond with an annual interest rate of 4%, compounded quarterly. How much will your investment be worth after 15 years?

$P_0 =$ _____ (initial deposit)

$r =$ _____ (4% annual rate)}

$k =$ _____ (4 quarters in a year)

$N =$ _____ (15 years)

The future value formula is:

$$P_n = P_0(1 + r/k)^{Nk}$$

Substituting the values: $P_n =$ _____ $(1 +$ _____ $/$ _____ $)^{Nk} =$ \$9024.80

Question

A retirement fund offers an annual interest rate of 4.5%, compounded annually, to help investors grow their savings. Suppose you contribute \$10,000 to this fund. How much will the account be worth after 12 years?

Example

You know that you will need \$25,000 for a down payment on a house in 15 years. If your account earns 3.5% interest compounded monthly, how much would you need to deposit now to reach your goal?

$$P_n = P_0(1+r/k)^{Nk}$$

$$P_0 = \frac{P_N}{(1+r/k)^{N \cdot k}}$$

$$P_0 = \frac{\underline{\hspace{2cm}}}{(1 + \underline{\hspace{1cm}} / \underline{\hspace{1cm}})^{\underline{\hspace{1cm}}}} = \$15,161.35$$

Question

You want to save \$30,000 for a car purchase in 5 years. If your savings account earns 6% interest compounded semiannually, how much do you need to deposit now to meet your goal?

1. Samantha borrows \$2,400, agreeing to pay it back with 1.5% annual interest after 15 months. How much interest will she pay?

2. A retiree invests \$5,000 in a savings plan that pays 4% per year. What will the account balance be at the end of the first year?

3. Evelyn invests \$15,000 into an account at an annual rate of 0.5% simple interest for 24 months.
 - a. What is the principal in this scenario?
 - b. What is the interest rate for this account?
 - c. What number do you use to represent the interest rate in the simple interest formula?
 - d. What is the length of time of this investment, in years?
 - e. Calculate the simple interest earned on this account.

4. You deposit \$500 in an account earning 6% interest compounded annually. How much will you have in the account in 10 years?