## Birthday Paradox

Suppose you have a room full of 30 people. What is the probability that there is at least one shared birthday?

Q. How many possible combinations of birthdays exist among the 30 people?

Q. How many combinations of birthdays among the 30 people leave no shared birthdays?

Q. What is the probability of no one sharing a birthday?

Q. What is the probability that there is at least one shared birthday?

## **Expected Value**

Expected Value is the average gain or loss of an event if the procedure is repeated many times.

We can compute the expected value by multiplying each outcome by the probability of that outcome, then adding up the products.

A company is considering launching a new product. Market research indicates

that there's a 60% chance of the product being successful and a 40% chance of it

failing. If the product succeeds, the company expects to make a profit of

\$500,000. However, if the product fails, the company anticipates a loss of

\$200,000. What is the expected value for the company in launching the new

 $E(X) = P_{success} \cdot X_{success} + P_{failure} \cdot X_{failure} =$ 

E(X) =

Example

product?

P<sub>success</sub>

 $P_{failure} =$ 

X<sub>success</sub> =

X<sub>failure</sub> =

=

## Example

You're participating in a local poker tournament with a buy-in of \$50. The tournament has 50 players. The prize pool is divided among the top 3 finishers, with the winner taking home \$1000, the second-place finisher receiving \$600, and the third-place finisher receiving \$300. Calculate the expected value of participating in this poker tournament.

X<sub>1</sub> = X<sub>2</sub> =

$$E(X) = X_1 \cdot P(X_1) + X_2 \cdot P(X_2) + X_3 \cdot P(X_3) + X_4 \cdot P(X_4)$$
  
=

- X<sub>3</sub> = X<sub>4</sub> =
- P<sub>1</sub> =
- P<sub>2</sub> =
- $P_3 = P_4 =$