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$$P(\text{genetic condition}) = 0.05 \quad \text{FALSE NEGATIVE: } P(\text{negative} \mid \text{genetic condition}) = 0.08$$

$$\text{FALSE POSITIVE: } P(\text{positive} \mid \text{no genetic condition}) = P(\overline{\text{negative}} \mid \overline{\text{genetic condition}}) = 0.02$$

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$$P(\overline{\text{genetic condition}}) = 0.95$$

$$P(\text{genetic condition}) = 0.05 \quad \text{FALSE NEGATIVE: } P(\text{negative} \mid \text{genetic condition}) = 0.08$$

$$\text{FALSE POSITIVE: } P(\text{positive} \mid \text{no genetic condition}) = P(\text{positive} \mid \overline{\text{genetic condition}}) = 0.02$$

$$P(\text{positive} \mid \text{genetic condition}) = 1 - P(\text{negative} \mid \text{genetic condition}) = 1 - 0.08 = 0.92$$

$$P(\text{genetic condition} \mid \text{positive}) = \frac{P(\text{genetic condition}) P(\text{positive} \mid \text{genetic condition})}{P(\text{genetic condition}) P(\text{positive} \mid \text{genetic condition}) + P(\overline{\text{genetic condition}}) P(\text{positive} \mid \overline{\text{genetic condition}})}$$

$$= \frac{0.05 \cdot 0.92}{(0.05 \cdot 0.92) + (0.95 \cdot 0.02)} \approx 0.7077$$

# BASIC COUNTING RULE

If we are asked to choose one item from each of two separate categories where there are  $m$  items in the first category and  $n$  items in the second category, then the total number of available choices is  $m \cdot n$ .

This is sometimes called the **multiplication rule for probabilities**.

# Example

Suppose you have 5 different colored shirts (red, blue, green, yellow, and black) and 4 different colored pants (orange, purple, gray, and brown) in your wardrobe.

You want to select one shirt and one pair of pants to wear for the day.

Total number of different outfits:

$$\begin{aligned} & \#(\text{shirts}) \cdot \#(\text{pants}) \\ & = 5 \cdot 4 = 20 \end{aligned}$$



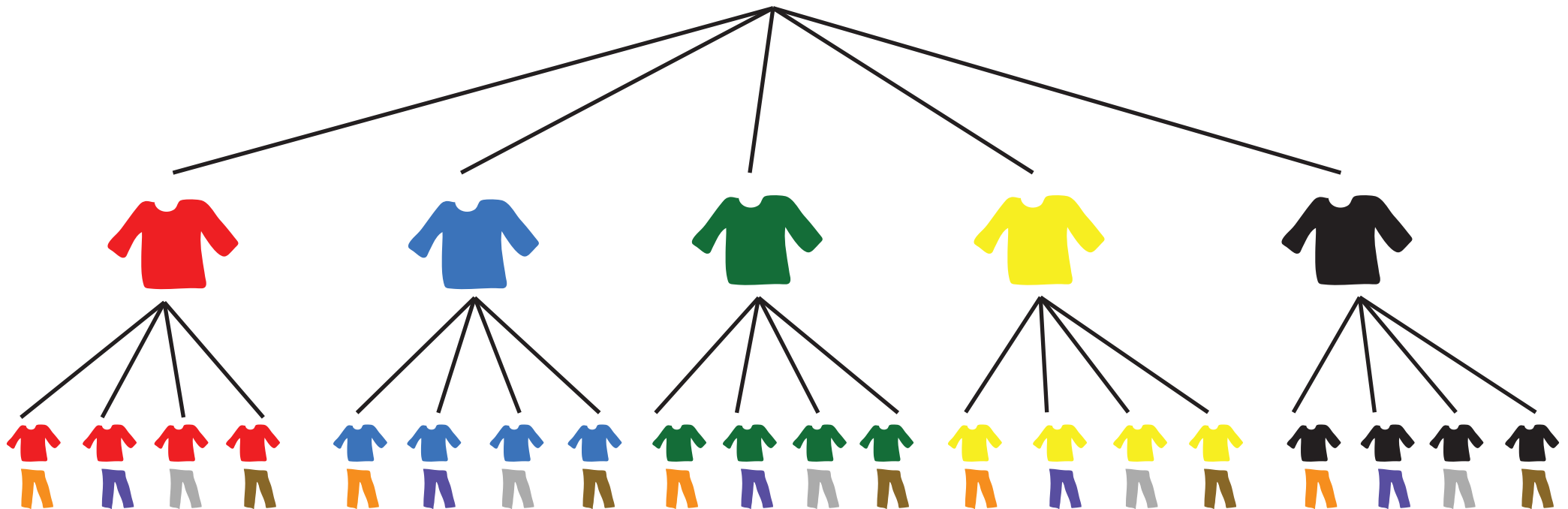
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## Example

Let's consider a scenario where you're organizing a sports event with different activities and teams.

Suppose you have the following options:

3 types of activities (football, basketball, volleyball)

4 teams (Team A, Team B, Team C, Team D)

2 time slots (morning, afternoon)

Total number of different combinations:  $\#(\text{options for activities}) \times \#(\text{options for teams}) \times \#(\text{options for time slots})$   
 $= 3 \cdot 4 \cdot 2 = 24$

Therefore, there are 24 different combinations considering the type of activity, team, and time slot.

## Question

You roll a dice 3 three times. how many possibilities are there in total?



## question

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Each roll has 6 possibilities.

total number of combinations =  $6 \cdot 6 \cdot 6 = 216$

## question

You flip a coin 4 times. How many possible outcomes are there in total?

## Question

How many combinations are there of a four digit numeric code?

## Question

You draw a card from a standard deck of 52 cards 2 times, with replacement. How many possible outcomes are there in total?

## Question

You spin a spinner with 8 equal sections 5 times. How many possible outcomes are there in total?

# Question

how many different ways can we order the numbers

1 2 3 4 5 ?

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1 2 3 4 5 ?

12345  
12354  
12435  
12453  
12534  
12543  
13245  
13254  
13425  
13452  
13524  
13542  
14235  
14253  
14325  
14352  
14523  
14532  
15234  
15243  
15324  
15342  
15423  
15432

21345  
21354  
21435  
21453  
21534  
21543  
23145  
23154  
23415  
23451  
23514  
23541  
24135  
24153  
24315  
24351  
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24531  
25134  
25143  
25314  
25341  
25413  
25431

31245  
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31542  
32145  
32154  
32415  
32451  
32514  
32541  
34125  
34152  
34215  
34251  
34512  
34521  
35124  
35142  
35214  
35241  
35412  
35421

41235  
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41352  
41523  
41532  
42135  
42153  
42315  
42351  
42513  
42531  
43125  
43152  
43215  
43251  
43512  
43521  
45123  
45132  
45213  
45231  
45312  
45321

51234  
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52143  
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53124  
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53412  
53421  
54123  
54132  
54213  
54231  
54312  
54321

# FACTORIAL

$$n! = n \cdot (n - 1) \cdot (n - 2) \cdots 3 \cdot 2 \cdot 1$$



## Question

Suppose there are 5 different tasks (A, B, C, D, E) to be assigned to 5 employees (Alice, Bob, Charlie, David, Emma) in a company.

How many ways can the tasks be assigned to the employees?

## Question

Suppose there are 7 different books to be placed on 7 different shelves in a library.

How many ways can the books be arranged on the shelves?

## Question

Suppose there are 5 different seats in a row, and 5 friends need to sit in those seats.

How many ways can the friends be seated?

## Question

Suppose there are 6 different colored balls (red, blue, green, yellow, purple, orange) to be placed into 6 distinct boxes.

How many ways can the balls be placed in the boxes?

## question

In a deck of 52 playing cards, how many different ways can you draw three cards in a specific order without replacement?

$$nPr = n \cdot (n - 1) \cdot (n - 2) \cdots (n - r + 1)$$

We say that there are  **$nPr$  permutations of size  $r$**  that may be selected from among  $n$  choices without replacement when order matters.

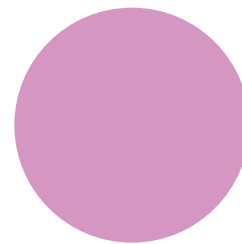
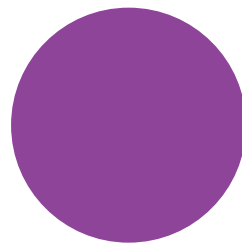
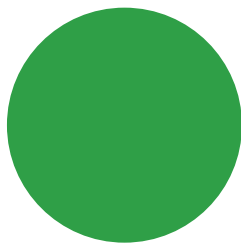
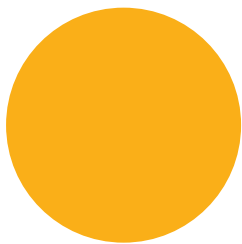
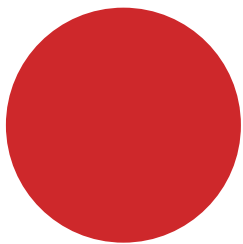
It turns out that we can express this result more simply using factorials.

$$nPr = \frac{n!}{(n-r)!}$$

## Question

How many different ways can 3 students be chosen and arranged from a group of 5 students?

$${}^5P_3 = \frac{5!}{(5-3)!} = \frac{5!}{2!} = \frac{5 \times 4 \times 3 \times 2 \times 1}{2 \times 1} = 60$$






# Question

A restaurant has 7 different types of desserts, and the chef wants to create a special dessert platter with 3 different desserts. How many different ways can the chef arrange these desserts?

# Question

A music festival features 9 different bands, and the organizer wants to schedule 4 of these bands to perform in a specific order. How many different ways can the organizer arrange these 4 bands?

## Question

I have twelve different types of plants, and I want to arrange only five of them in a row on my garden bed. How many different ways could I do this?

# COMBINATIONS

$${}^n C_r = \frac{n!}{(n-r)! r!}$$

# Question

How many ways can I choose 3 socks from a drawer containing 23 socks?

# Question

In a group of 10 students, how many different ways can we choose a committee of 3 students to represent the class?

## Question

A pizza restaurant offers 10 different toppings. How many different combinations of 5 toppings can a customer choose for their pizza?

## Question

A sports team has 15 players, and the coach needs to select 4 players to represent the team in a tournament. How many different ways can the coach choose the players?